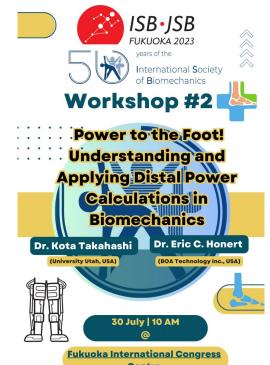
# Power to the Foot! Understanding and Applying Distal Power Calculations in Biomechanics



Eric Honert & Kota Takahashi

Our Slack link:

https://tinyurl.com/ISBfootpower

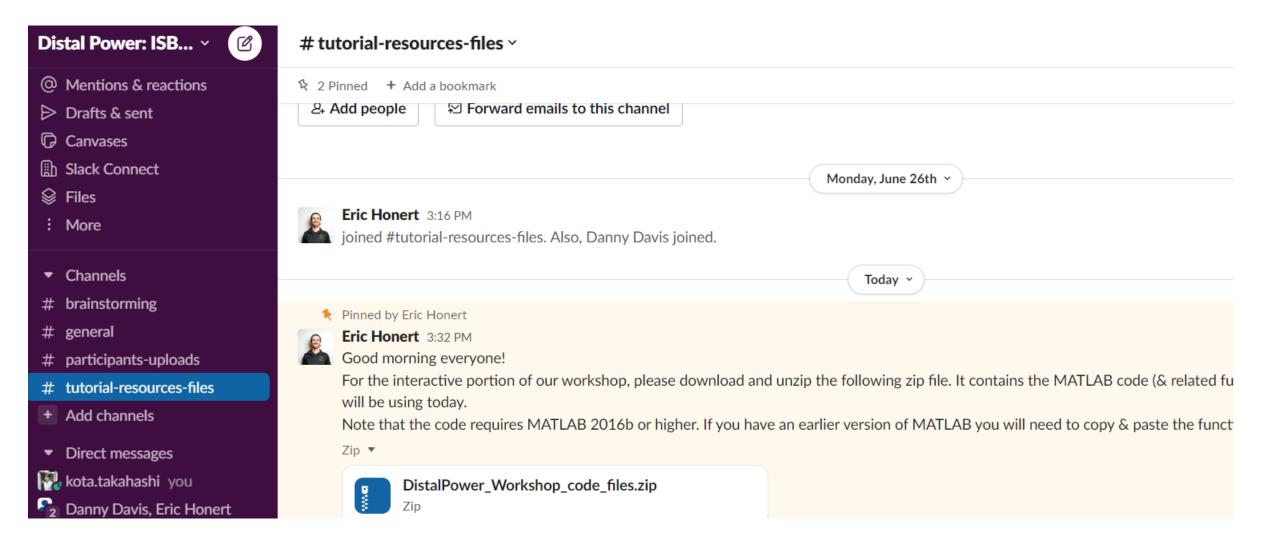


# Join our Slack workspace

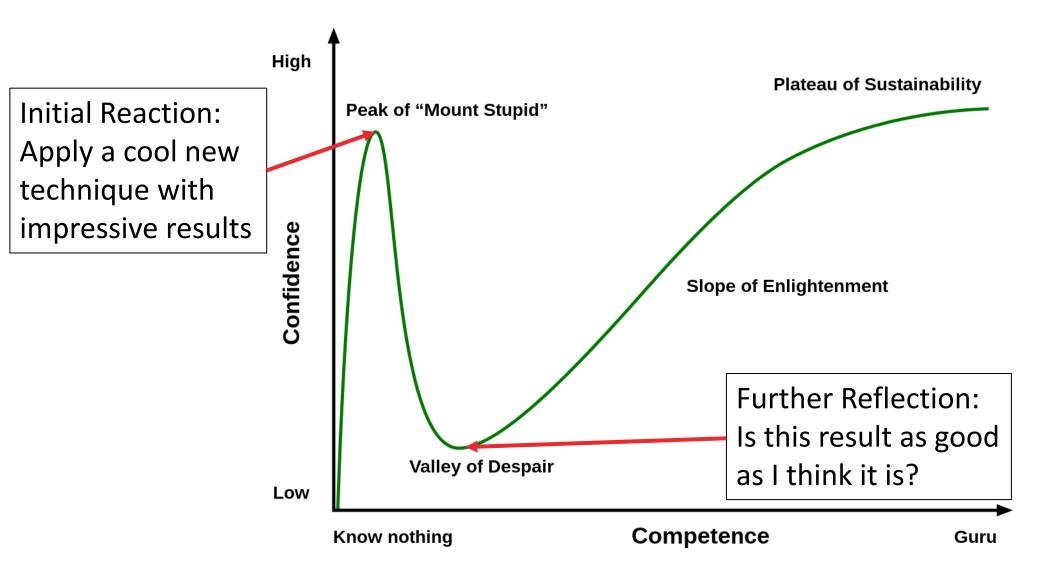
https://tinyurl.com/ISBfootpower



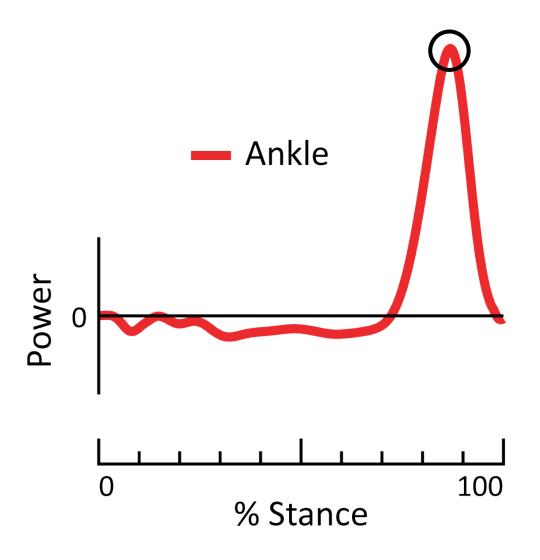
### Tutorial Resources – via Slack



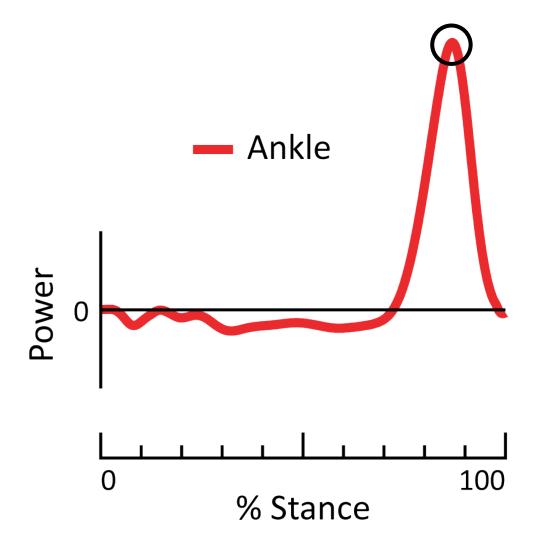
# Dunning-Kruger of Methodologies



### Beneficial Ankle Push-off



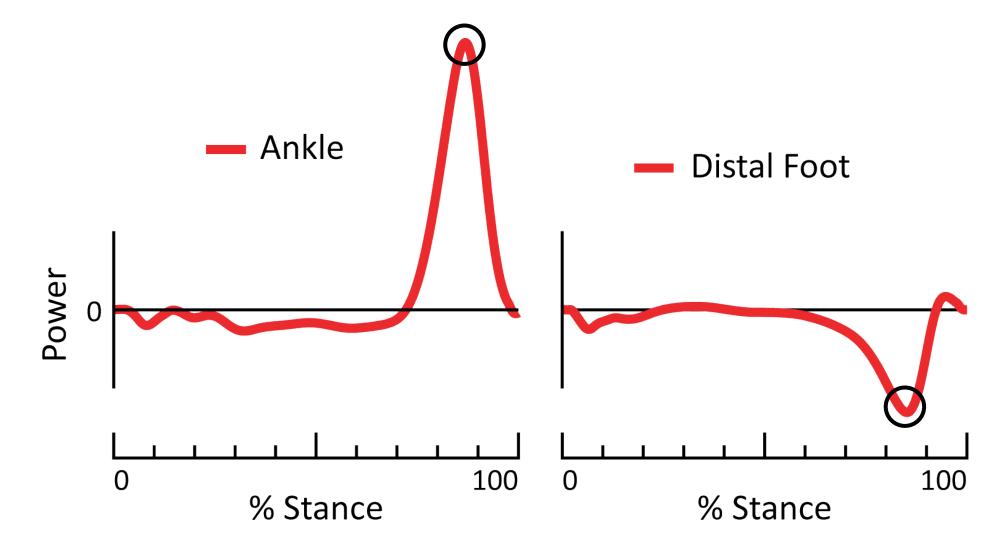
### Beneficial Ankle Push-off



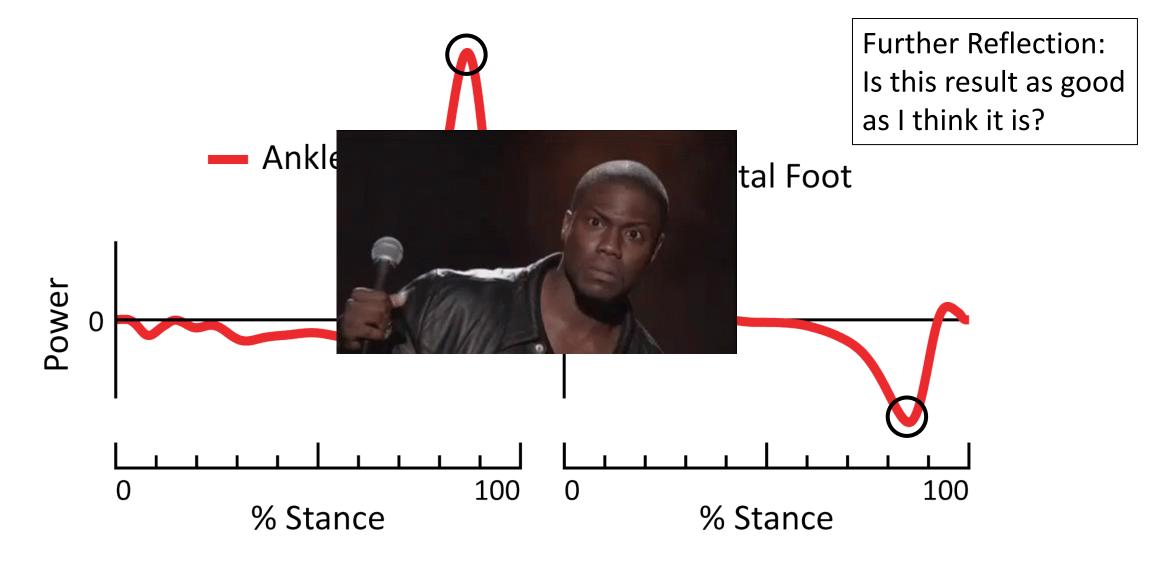


Initial Reaction:
Apply a cool new technique
with impressive results

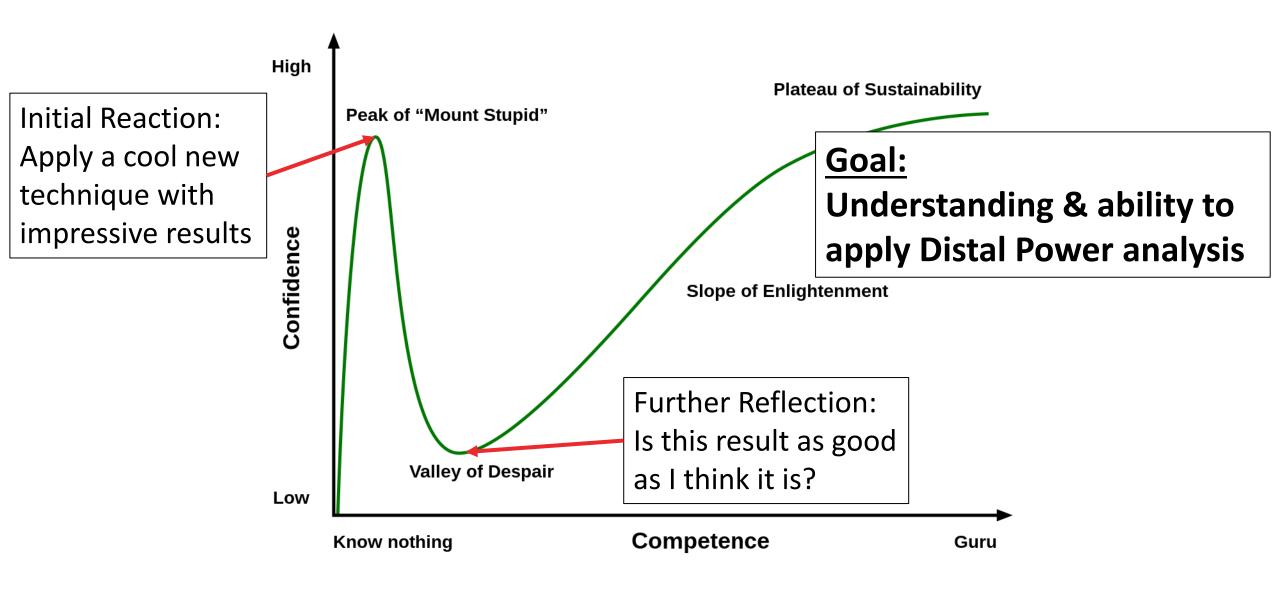
### Ankle Push-off with Foot Absorption?



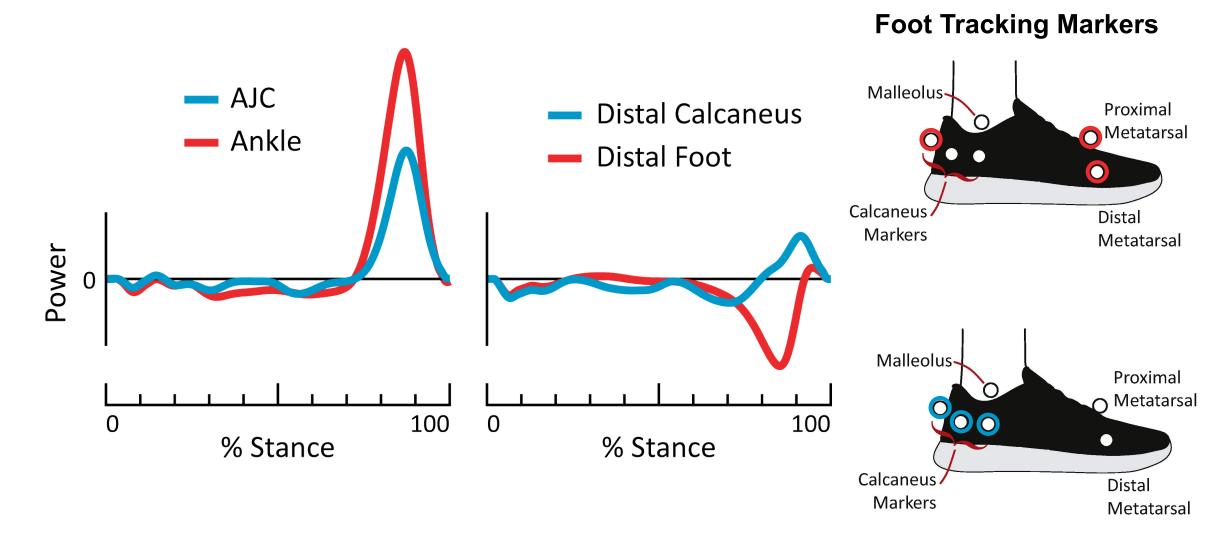
### Ankle Push-off with Foot Absorption?



# Workshop Goal: Slope of Enlightenment



### Understanding the Ankle & Foot



### Workshop Outline

- Current Distal power Applications
- Two Perspectives on the Methodology
- Applying the Distal power
- Future Applications

# Application: Understanding Footwear



Brooks Hyperion Elite 2



Nike VaporFly



**HOKA ONE ONE Carbon X 2** 



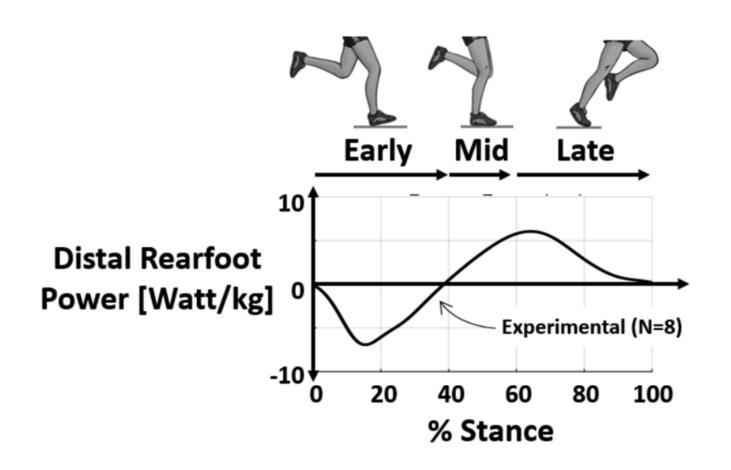
Adidas Adizero Adios Pro



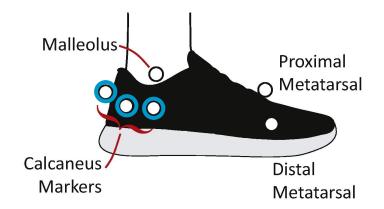
Nike AlphaFly

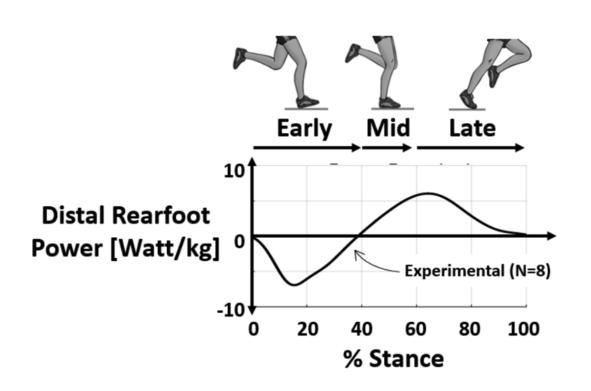


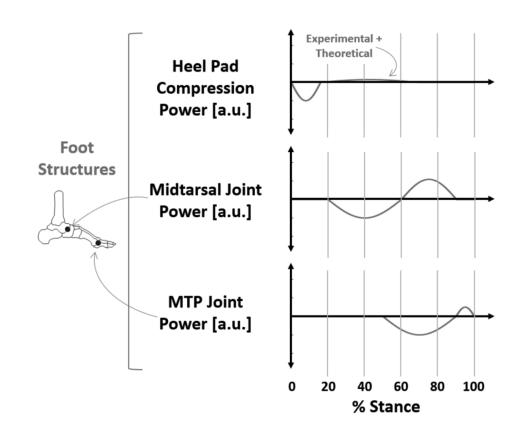
Saucony Endorphin Pro

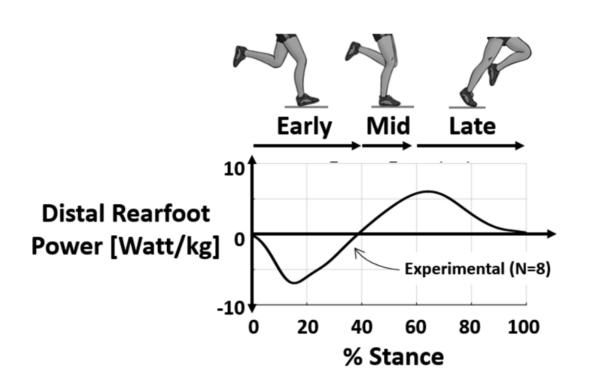


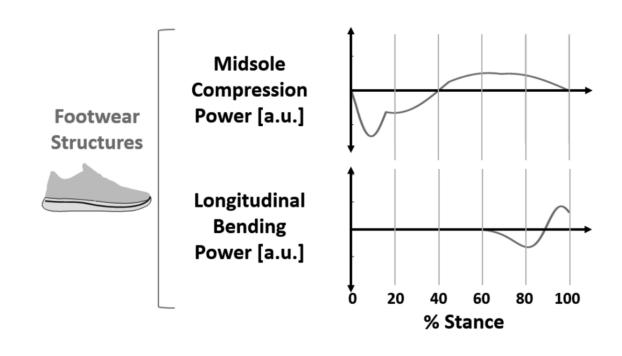
#### **Foot Tracking Markers**



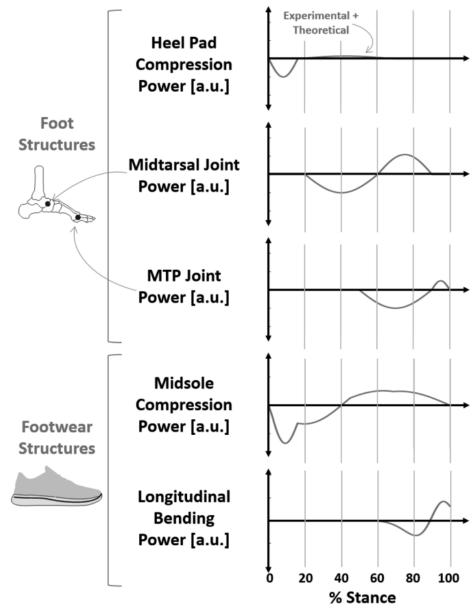


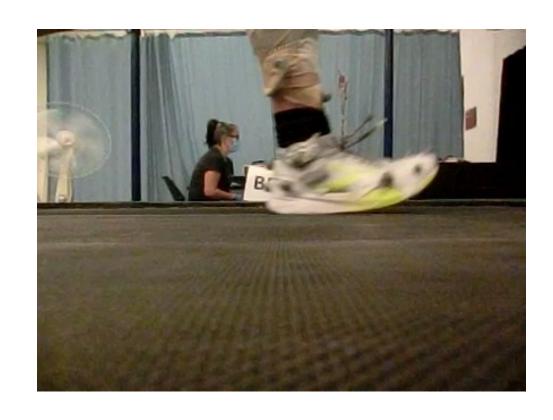


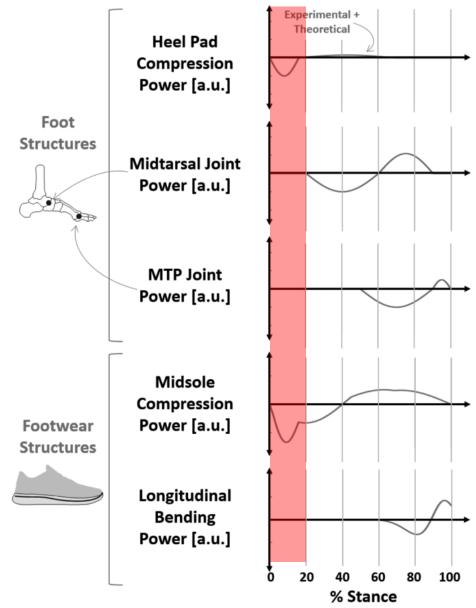




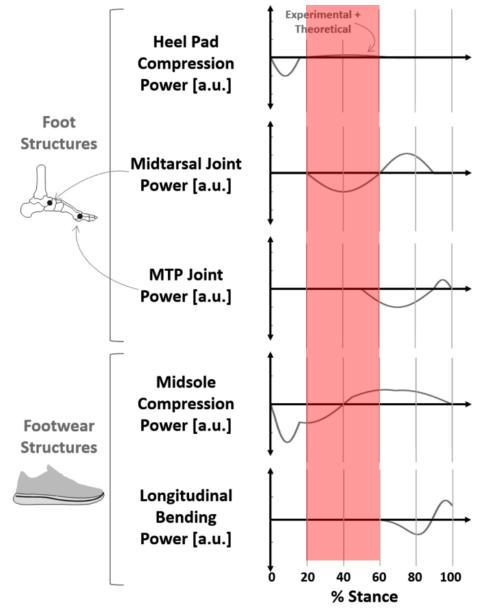




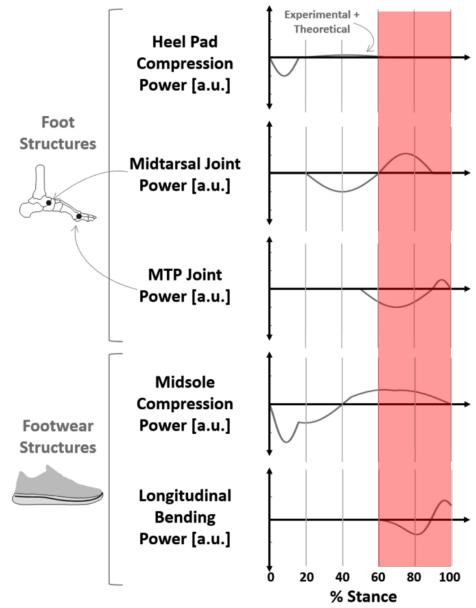




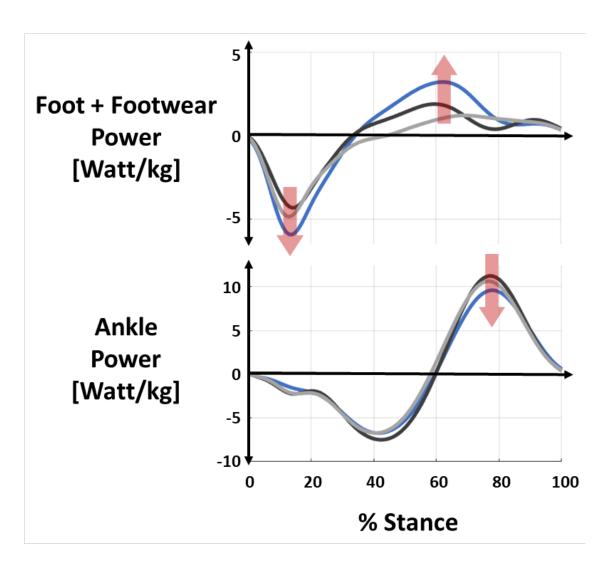








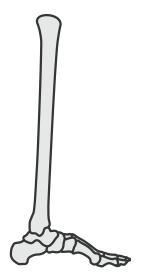
### Advanced Footwear: Offset Ankle Work





Matijevich et al. 2023, *In Review* 

Combined Foot Power (Distal Rearfoot)

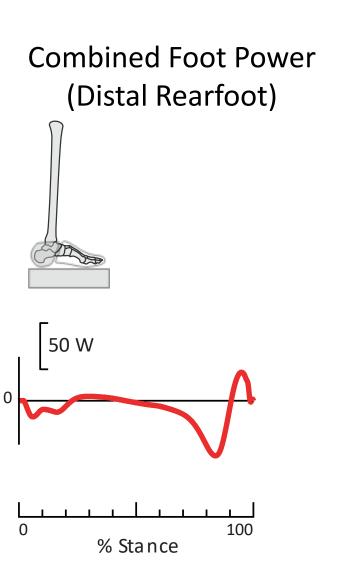


Combined Foot Power (Distal Rearfoot)



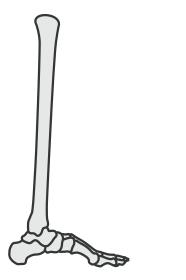
**Combined Foot Power** (Distal Rearfoot) 50 W 100

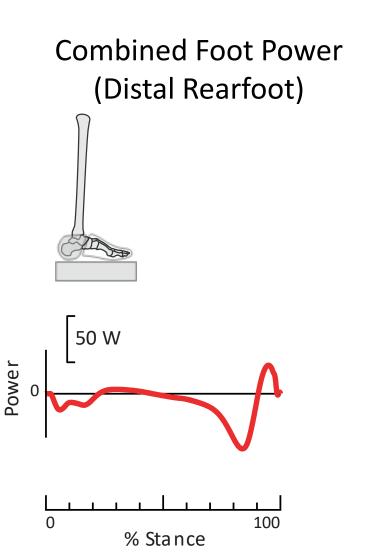
% Stance



Power

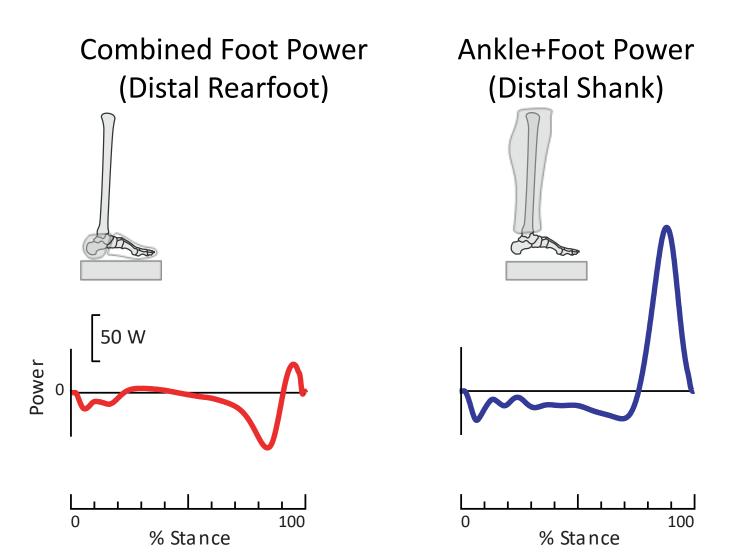
Ankle+Foot Power (Distal Shank)



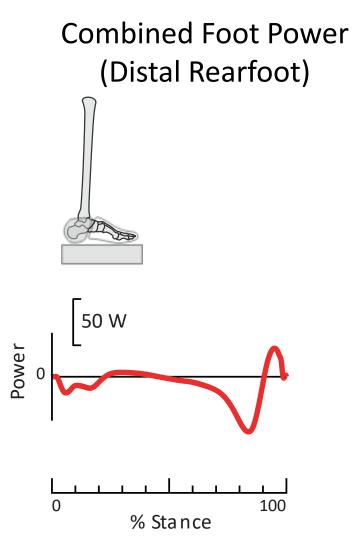


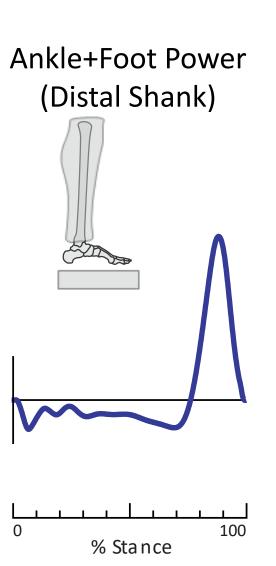
Ankle+Foot Power (Distal Shank)





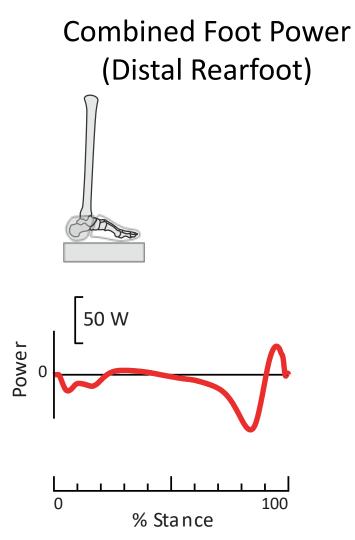
#### Same Methods: Prosthesis Contributions

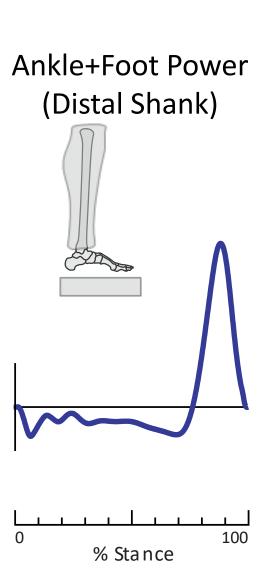






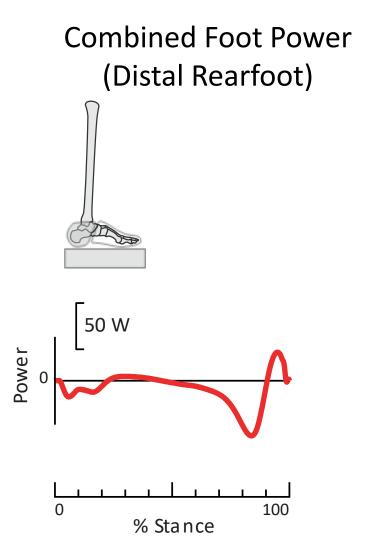
#### Same Methods: Prosthesis Contributions

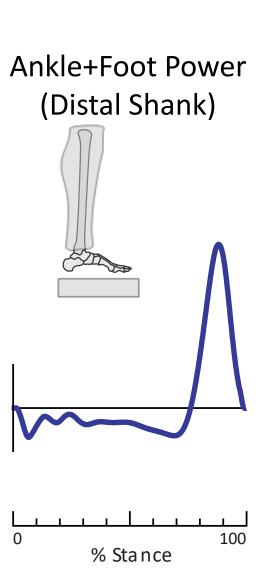


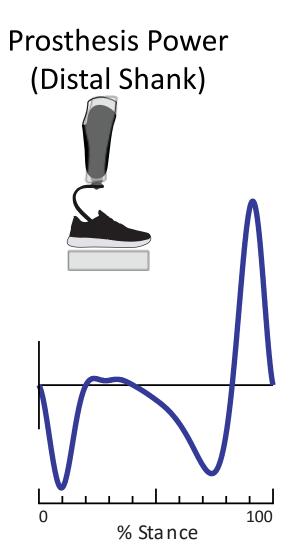




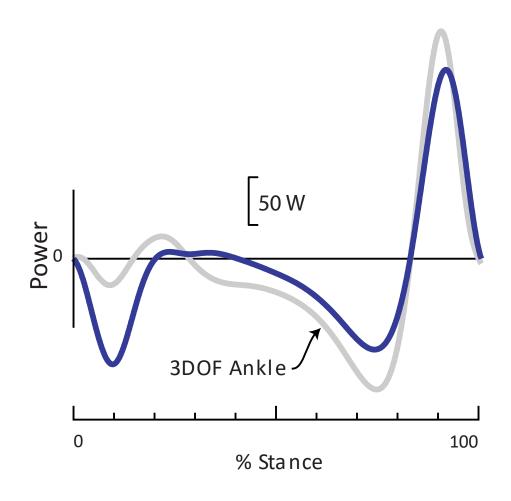
#### Same Methods: Prosthesis Contributions



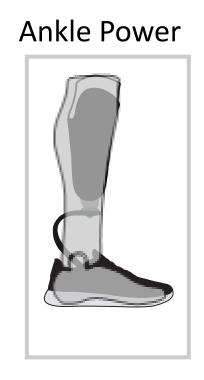




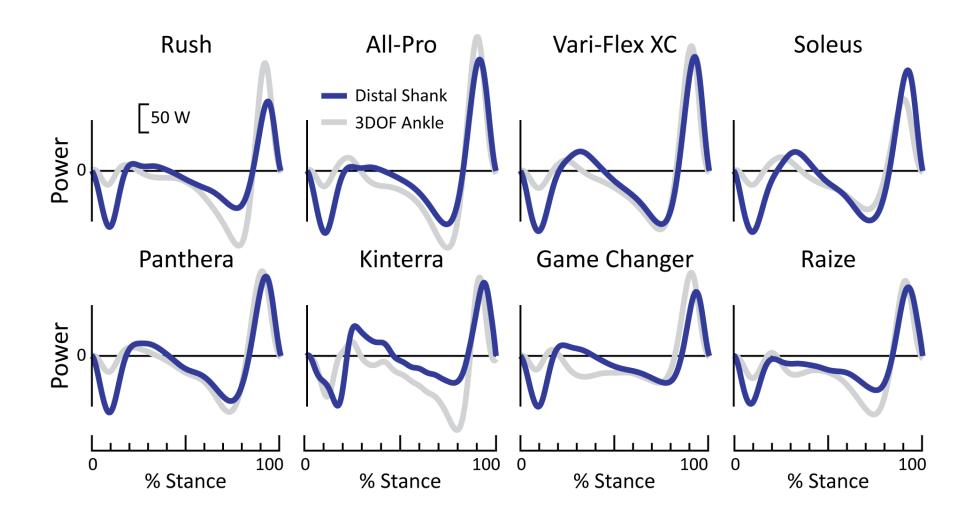
### Comparison to "Traditional" Estimates



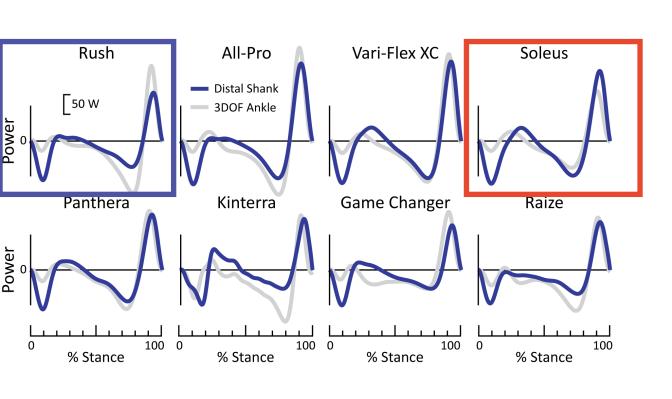


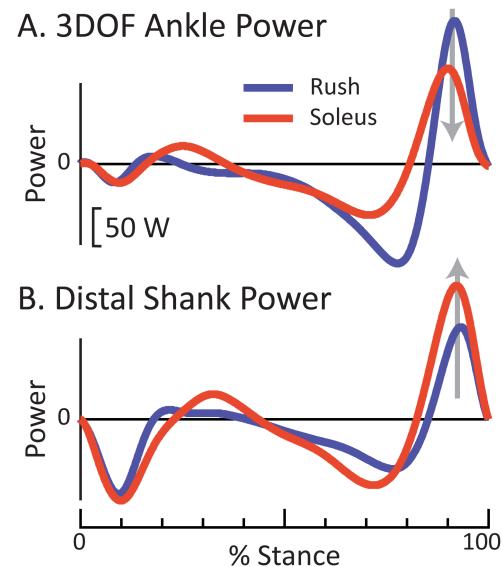


#### "Traditional" Methods can Mis-Estimate Prosthesis Contributions



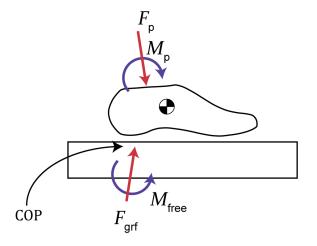
### ...which may skew interpretations





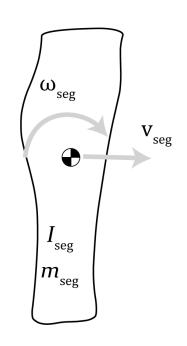
### 'Distal power' as an extension of segment power

(and a brief history of 'power imbalance' in biomechanics)



### Segment power can be quantified in two ways:

#### 1) Kinematic method:

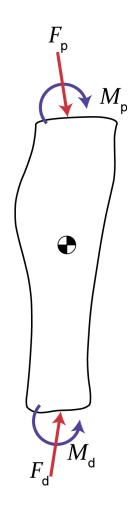


$$E_{seg} = \frac{1}{2} m \vec{v}^2 + \frac{1}{2} I \vec{\omega}^2 + mgh$$
 Kinetic Energy Potential Energy

$$\dot{E}_{seg} = P_{seg}$$

(Rate of Energy Change = Segment Power)

### Segment power can be quantified in two ways:



#### 2) Kinetic method:

$$P_{seg} = \overrightarrow{M}_p \cdot \overrightarrow{\omega}_p + \overrightarrow{F}_p \cdot \overrightarrow{v}_p + \overrightarrow{M}_d \cdot \overrightarrow{\omega}_d + \overrightarrow{F}_d \cdot \overrightarrow{v}_d$$
 Proximal Seg. Terms Distal Seg. Terms

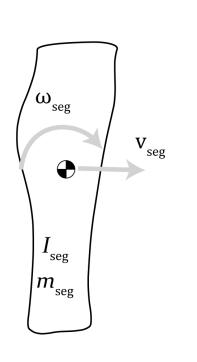
 $\overrightarrow{M} \& \overrightarrow{F}$ : (from inverse dynamics)

 $\vec{v} \& \vec{\omega}$ : (from MoCap)

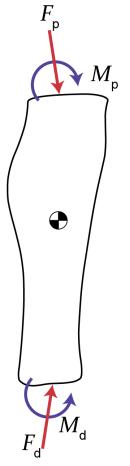
### In theory, these two methods should match...

(i.e., power balance)

Kinematics method

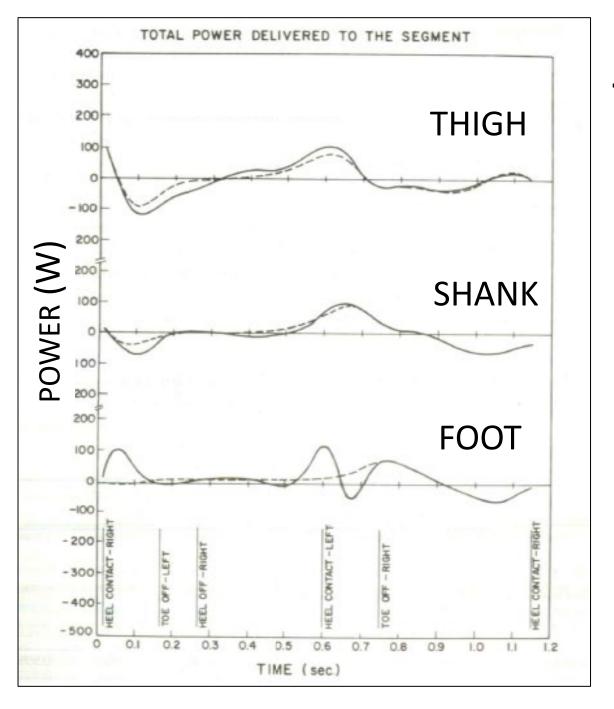






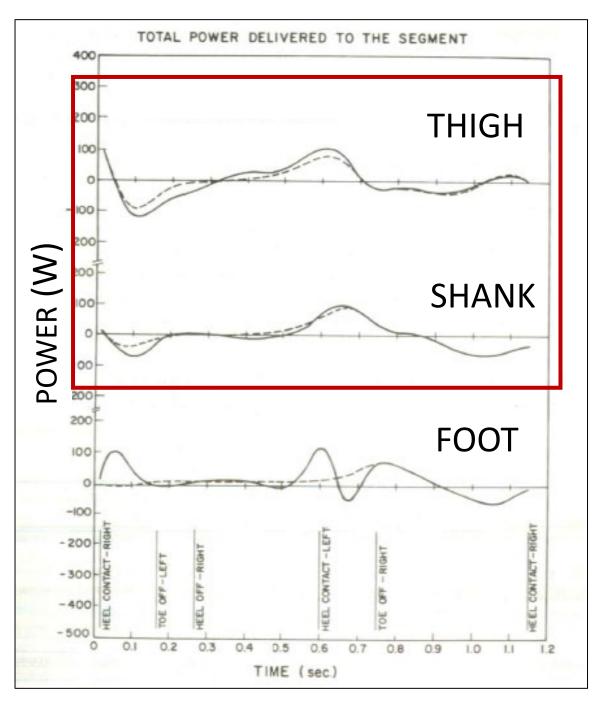
Kinetics method

$$\dot{E}_{seg} = P_{seg}$$



- --- Kinematic method
- Kinetic method

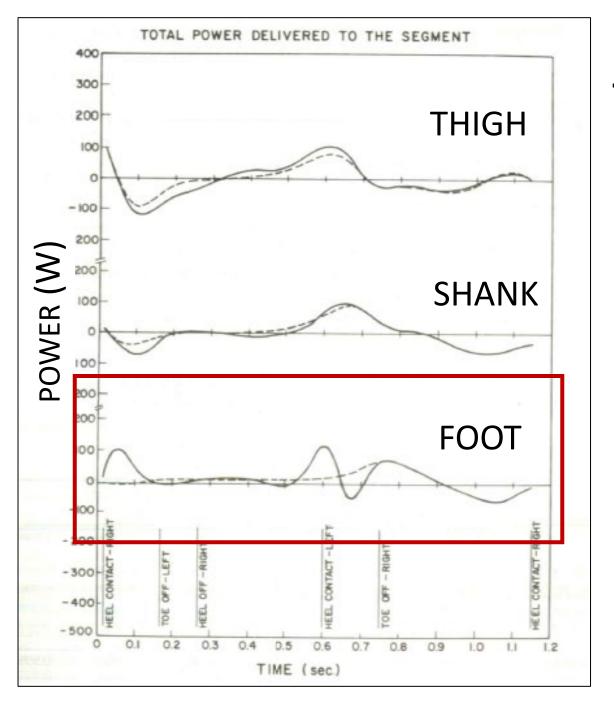
Robertson DG and Winter DA, 1980 Journal of Biomechanics



- --- Kinematic method
- Kinetic method

# Good agreement at the thigh and shank

Robertson DG and Winter DA, 1980 Journal of Biomechanics

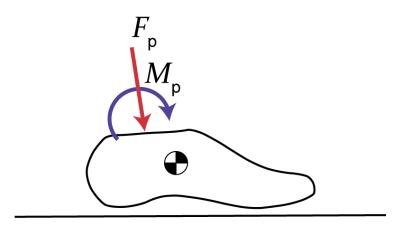


- --- Kinematic method
- Kinetic method

# 'Power imbalance' at the foot!

Robertson DG and Winter DA, 1980 Journal of Biomechanics

### Imbalance due to lack of 'distal power' terms at the foot

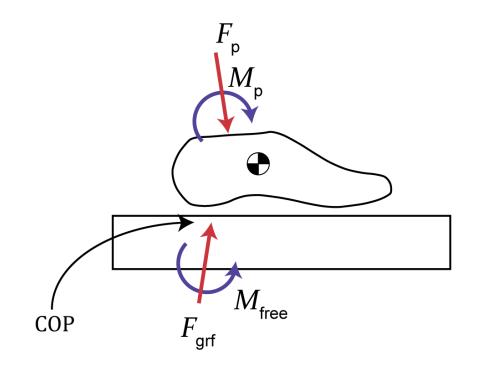


#### **Assumptions**:

The foot is rigid & foot did not slip....

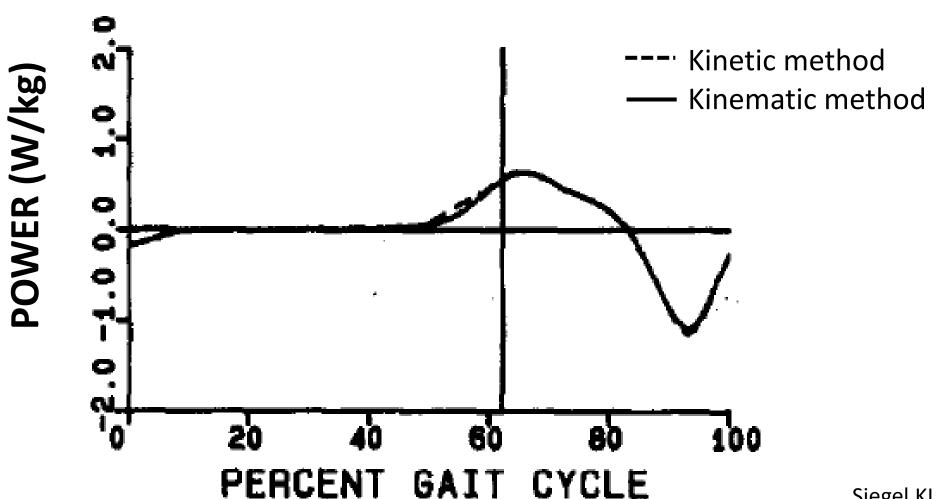
- Distal velocity  $(\vec{v}_d)$ = 0
- Distal power = 0

### Adding 'distal' terms achieves power balance at the foot



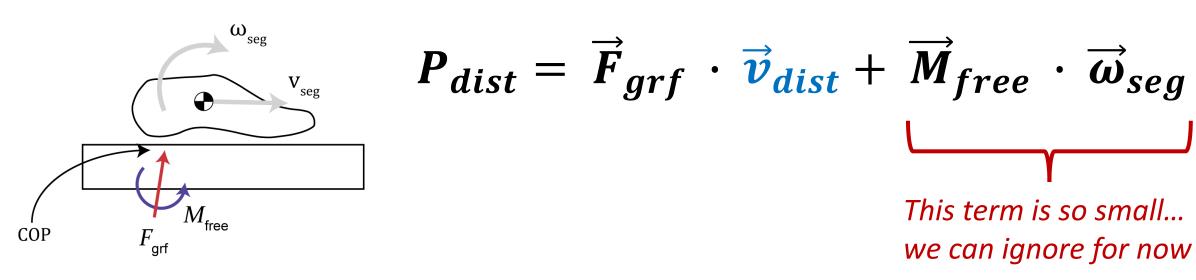
$$\vec{F}_d = \vec{F}_{grf}$$
  $\vec{M}_d = \vec{M}_{free}$ 

### Adding 'distal' terms achieves power balance at the foot

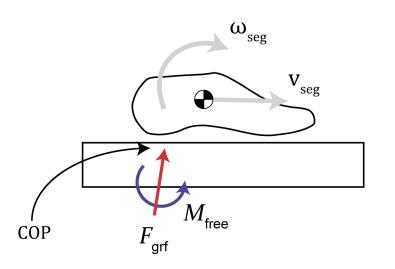


Siegel KL et al, 1996
Journal of Biomechanics

## So, what exactly is this 'distal power' $(P_{dist})$ ?



## So, what exactly is this 'distal power' $(P_{dist})$ ?

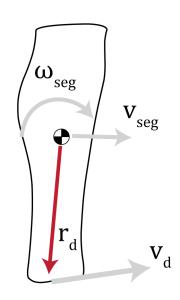


$$P_{dist} = \overrightarrow{F}_{grf} \cdot \overrightarrow{v}_{dist} + \overrightarrow{M}_{free} \cdot \overrightarrow{\omega}_{seg}$$

$$\vec{v}_{dist} = \vec{v}_{seg} + (\vec{\omega}_{seg} \times \vec{r}_{dist})$$

### Consider a rigid body segment translating and rotating in space...

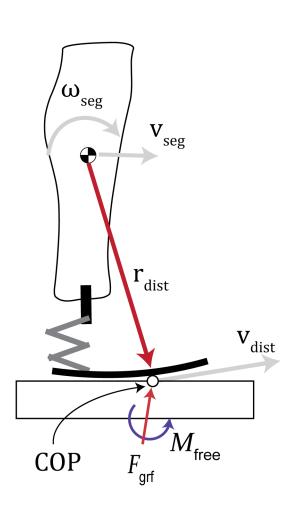




$$\vec{v}_d = \vec{v}_{seg} + (\vec{\omega}_{seg} \times \vec{r}_d)$$

 $st \vec{r}_d$  will be a constant for a rigid body

### Now, a rigid body segment with a deforming distal component...



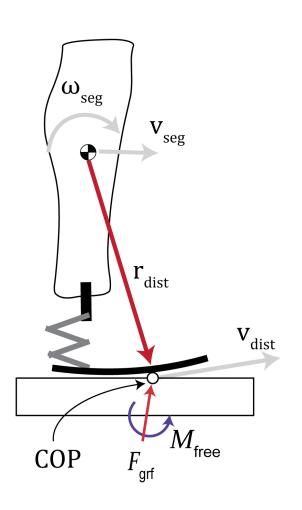
'Distal' velocity ( $\vec{v}_{dist}$ ):

$$\vec{v}_{dist} = \vec{v}_{seg} + (\vec{\omega}_{seg} \times \vec{r}_{dist})$$

 $(\vec{r}_{dist}$  - displacement of COP relative to COM)

\*  $\vec{r}_{dist}$  is a non-constant value

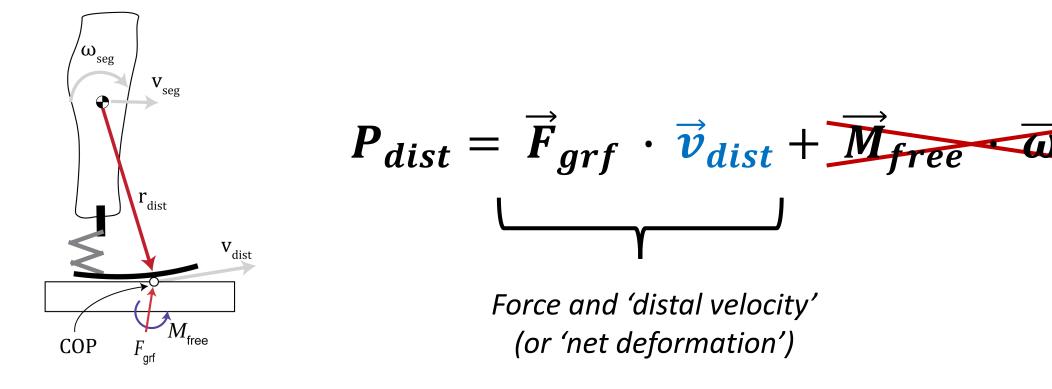
### Now, a rigid body segment with a deforming distal component...



$$\vec{v}_{dist} = \vec{v}_{seg} + (\vec{\omega}_{seg} \times \vec{r}_{dist})$$

$$P_{dist} = \overrightarrow{F}_{grf} \cdot \overrightarrow{v}_{dist} + \overrightarrow{M}_{free} \overrightarrow{w}_{seg}$$

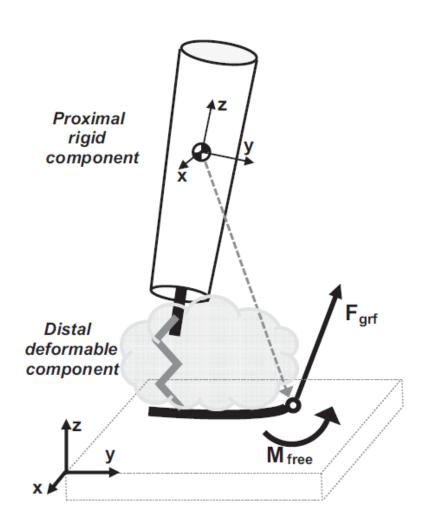
Force and 'distal velocity' (or 'net deformation')



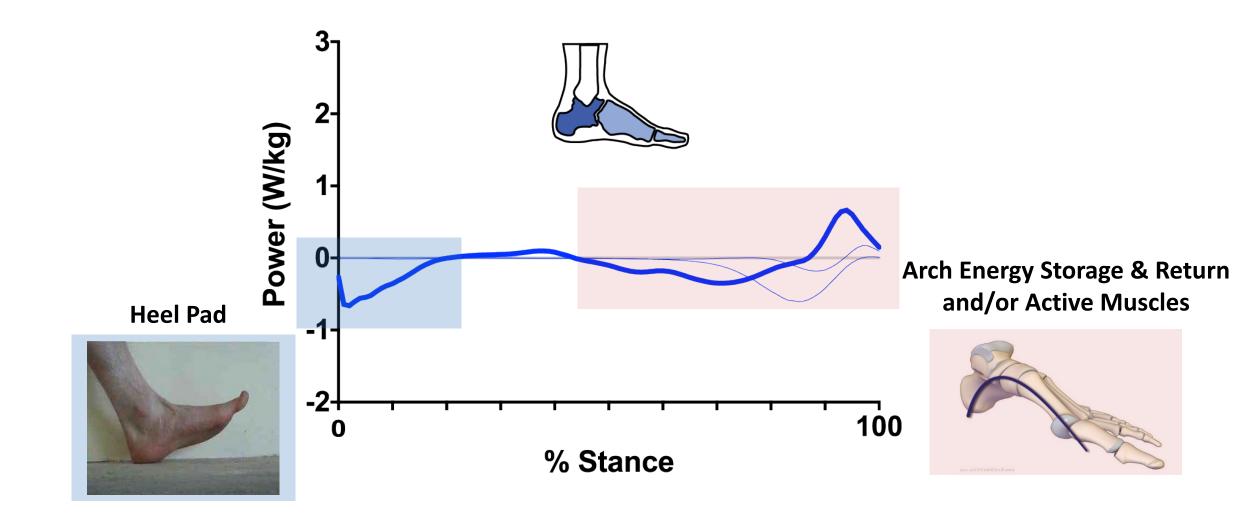
Generalized equation that can be applied to different segments

- Summed effects of all structures distal to a chosen segment
- No need to define 'joint' centers
- Inertial parameters not needed

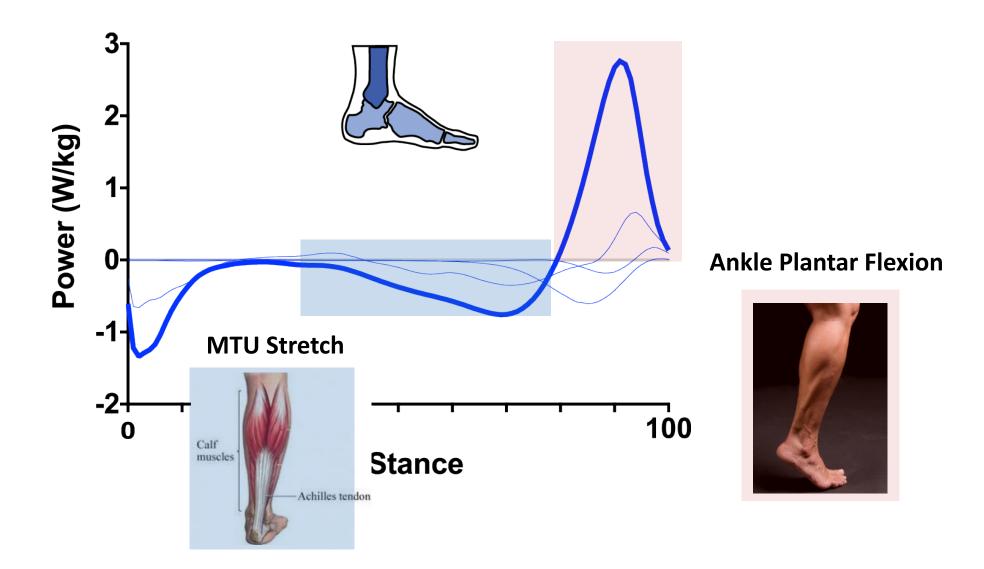
#### Unified Deformable (UD) Segment Power



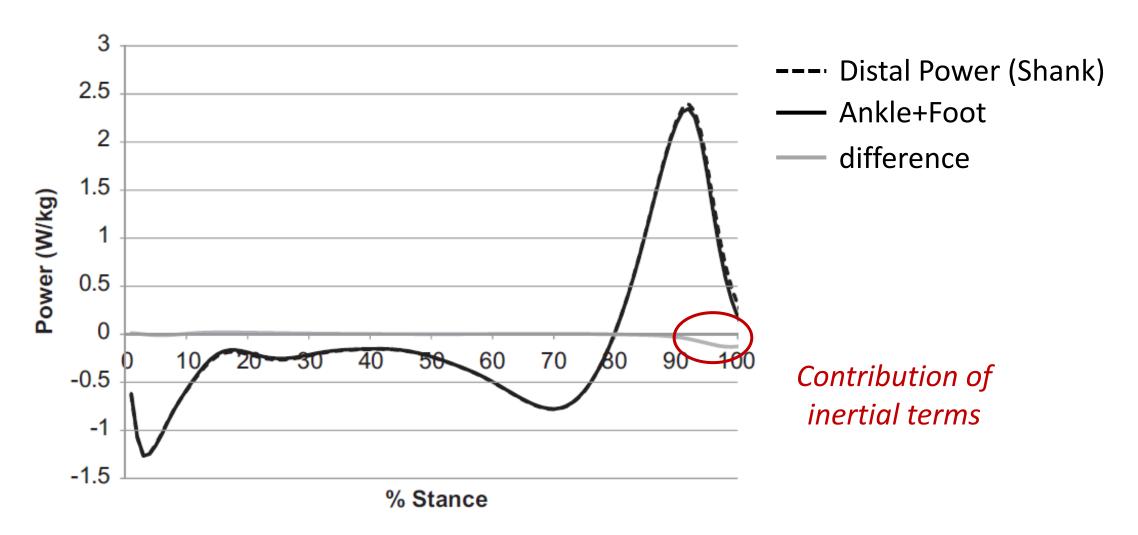
### Hindfoot (i.e., entire foot)



## Shank (i.e., ankle+foot)



### Distal power (at shank) is nearly equal to 'ankle+foot' power



Takahashi KZ, Kepple TM, Stanhope SJ 2012, Journal of Biomechanics

### Limitations of 'distal power' method

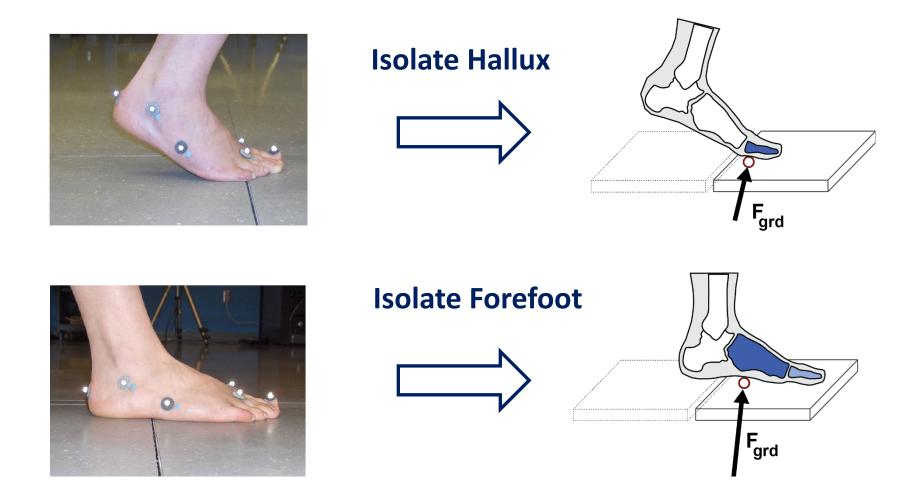
#### Misses inertial contributions

- Swing phase = 0
- Errors propagate when applying to proximal segments

#### Sums the effects of all distal structures

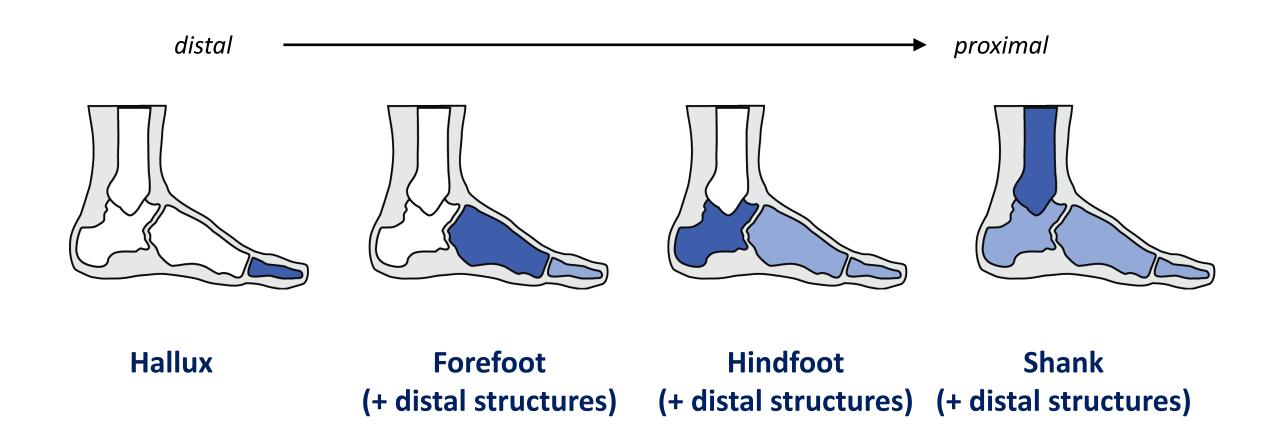
 Cannot partition contributions of isolated structures (without additional techniques)

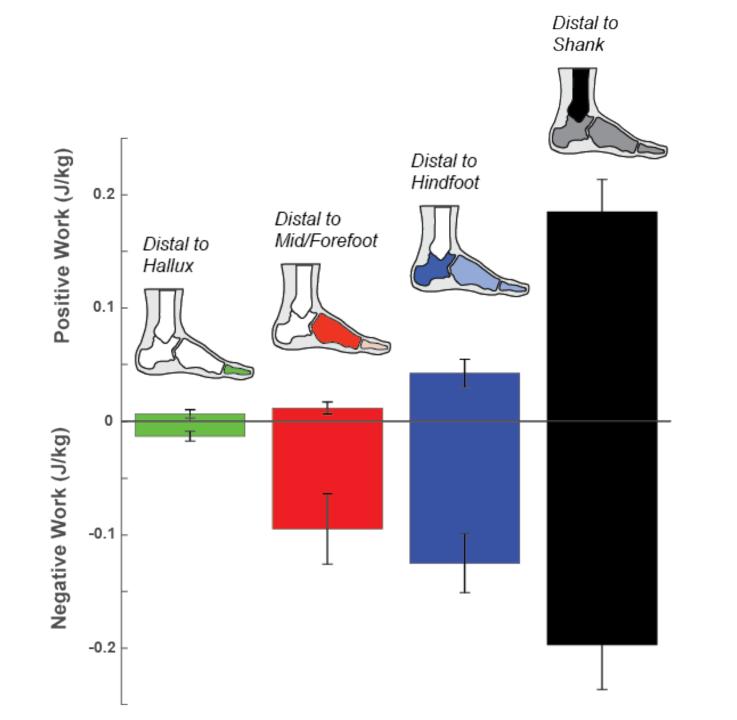
### Partitioning power from isolated regions



[Takahashi KZ, Worster K, Bruening DA 2017 Scientific Reports; Bruening DA and Takahashi KZ 2018 Gait & Posture]

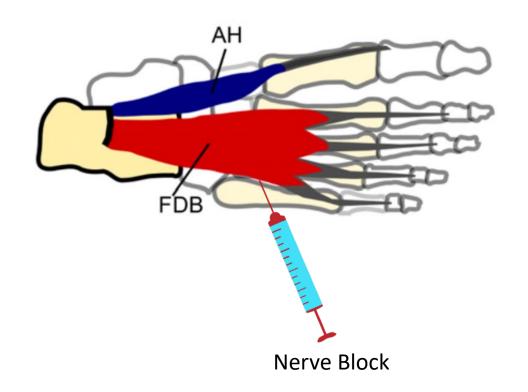
### Partitioning power from isolated regions





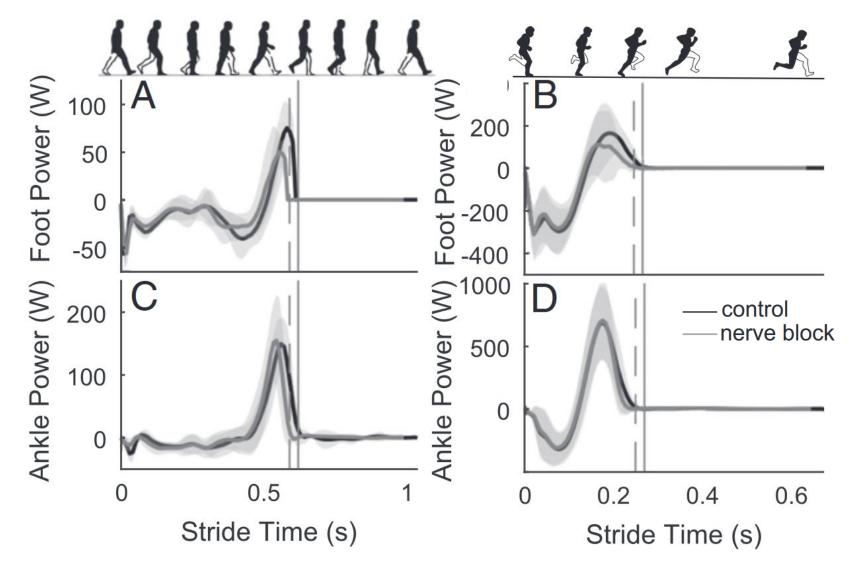
### Isolating role of intrinsic foot muscles





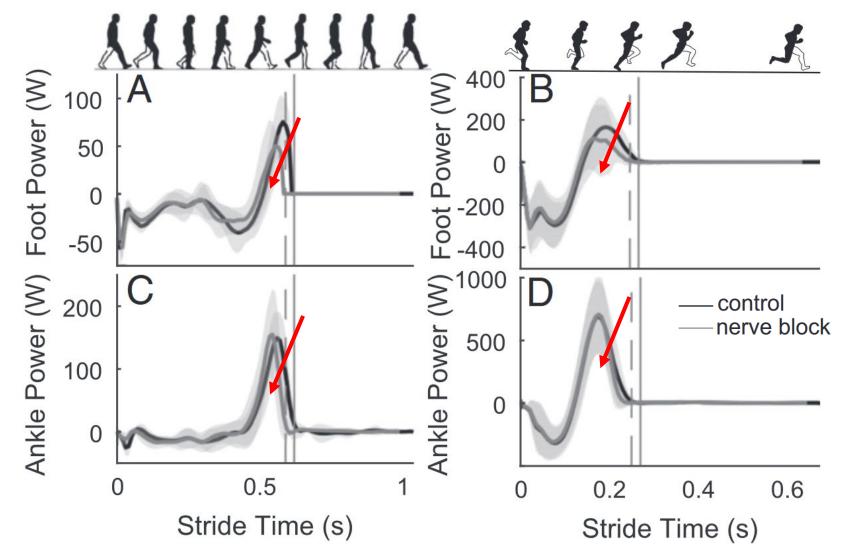
Farris et al., 2019 N=12

### Isolating role of intrinsic foot muscles



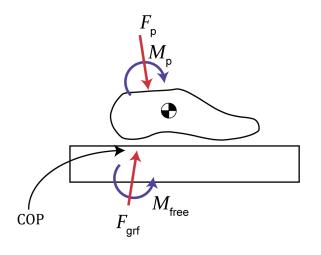
Farris et al., 2019 N=12

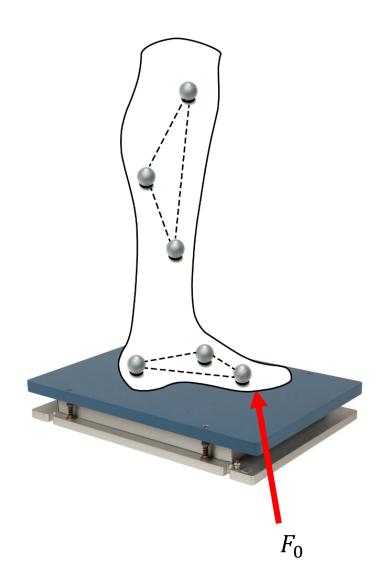
#### No foot muscles: Reduced Foot & Ankle Power



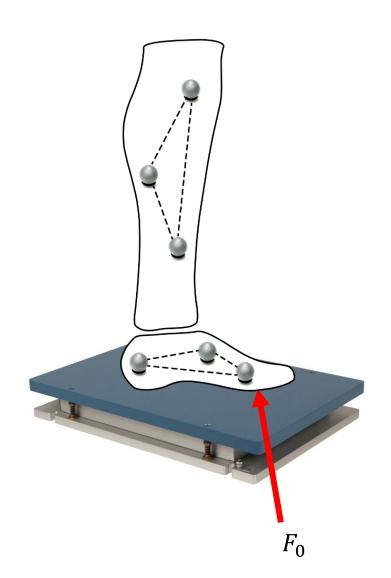
Farris et al., 2019 N=12

## 'Distal power' as an extension of joint power

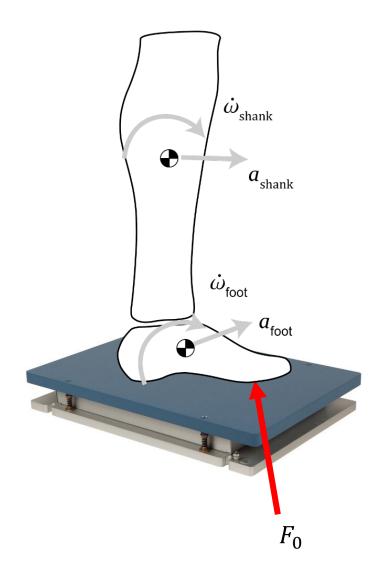




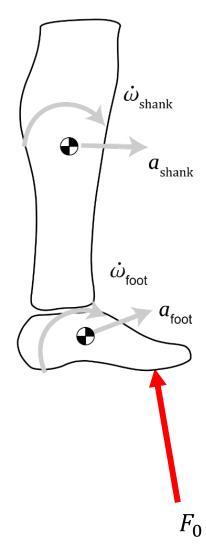






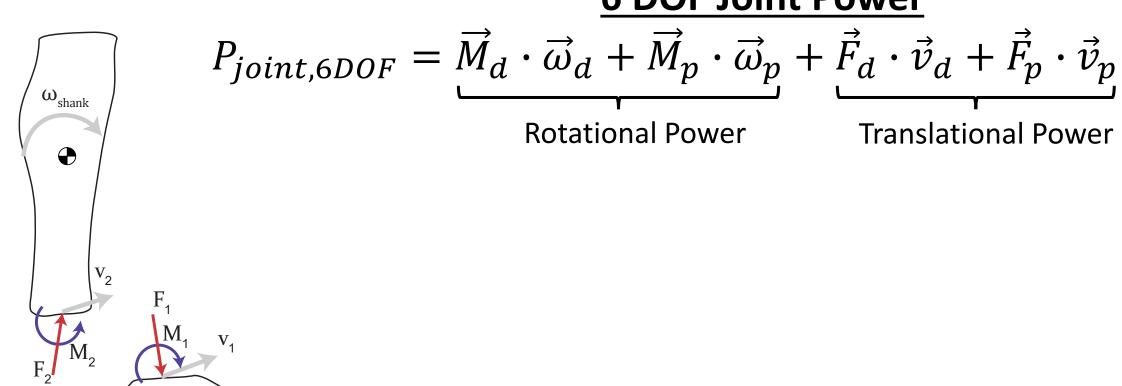




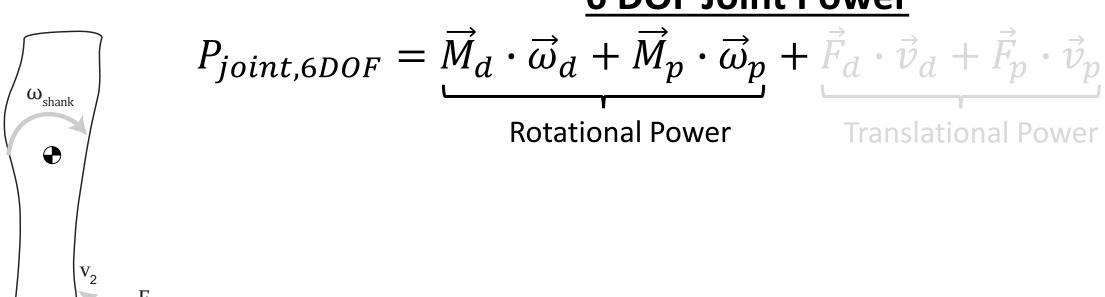


$$\sum \vec{F} = m \cdot \vec{a}$$

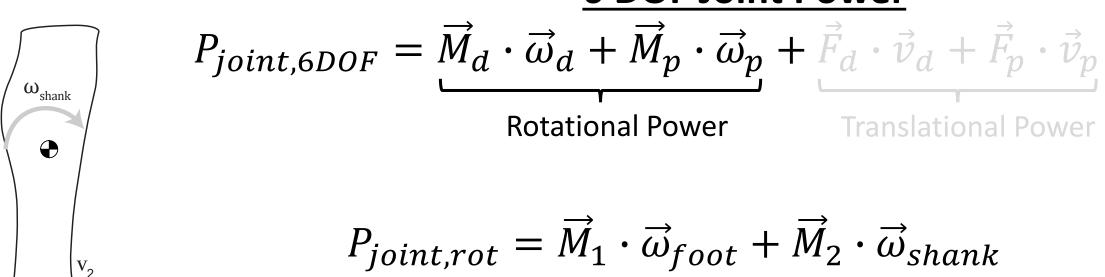
$$\sum \vec{M} = I \cdot \dot{\vec{\omega}}$$

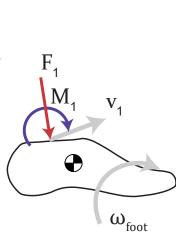


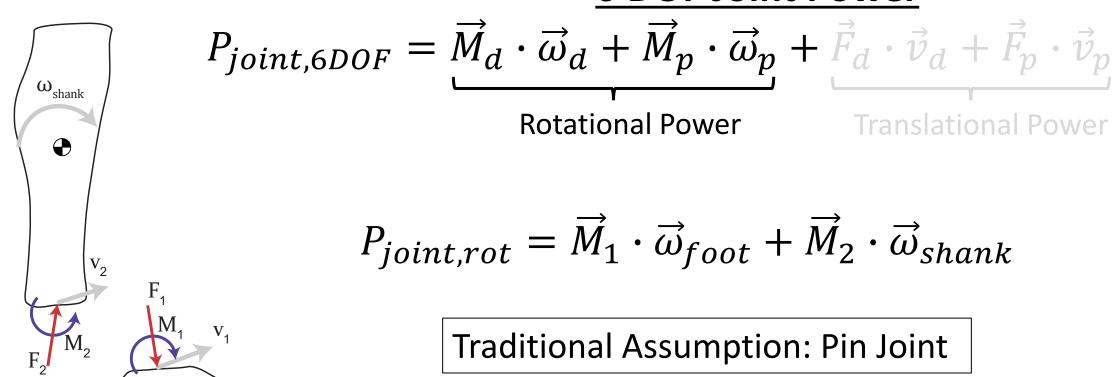
 $\omega_{\text{foot}}$ 



 $\omega_{\text{foot}}$ 







 $\omega_{\text{foot}}$ 

**Traditional Assumption: Pin Joint** 

$$\vec{M}_1 = -\vec{M}_2$$

$$P_{joint,rot} = \vec{M}_1 \cdot (\vec{\omega}_{foot} - \vec{\omega}_{shank})$$

#### **Rotational Component Joint Power**

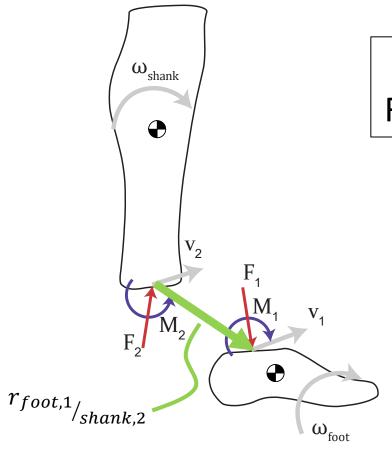
$$P_{joint,rot} = \vec{M}_1 \cdot \vec{\omega}_{foot} + \vec{M}_2 \cdot \vec{\omega}_{shank}$$



Foot & Shank Joint Centers may not be Coincident

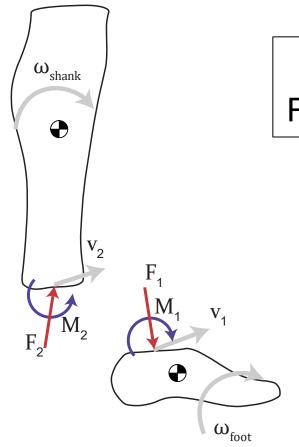
$$\sum \vec{M} = I \cdot \dot{\vec{\omega}}$$

$$\vec{M}_2 + \vec{M}_1 + \vec{r}_{foot,1} \times \vec{F}_1 = 0$$



#### **Rotational Component Joint Power**

$$P_{joint,rot} = \vec{M}_1 \cdot \vec{\omega}_{foot} + \vec{M}_2 \cdot \vec{\omega}_{shank}$$



**6DOF Assumption:** 

Foot & Shank Joint Centers may not be Coincident

$$\sum \vec{M} = I \cdot \dot{\vec{\omega}}$$

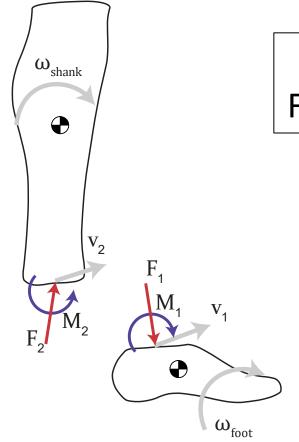
$$\vec{M}_{2} + \vec{M}_{1} + \vec{r}_{foot,1} \times \vec{F}_{1} = 0$$

$$\vec{M}_{2} = -\vec{M}_{1} + \vec{r}_{shank,2} \times \vec{F}_{1} \times \vec{F}_{1}$$

$$P_{joint,rot} = \vec{M}_1 \cdot \vec{\omega}_{foot} + (-\vec{M}_1 + \vec{r}_{shank,2}) \times \vec{F}_1 \cdot \vec{\omega}_{shank}$$

#### **Rotational Component Joint Power**

$$P_{joint,rot} = \vec{M}_1 \cdot \vec{\omega}_{foot} + \vec{M}_2 \cdot \vec{\omega}_{shank}$$



#### **6DOF Assumption:**

Foot & Shank Joint Centers may not be Coincident

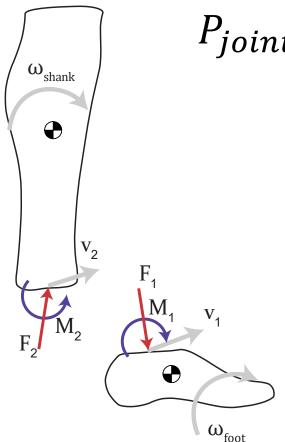
$$\sum \vec{M} = I \cdot \dot{\vec{\omega}}$$

$$\vec{M}_{2} + \vec{M}_{1} + \vec{r}_{foot,1} \times \vec{F}_{1} = 0$$

$$\vec{M}_{2} = -\vec{M}_{1} + \vec{r}_{shank,2} \times \vec{F}_{1}$$

$$\times \vec{F}_{1} = 0$$

$$P_{joint,rot} = \vec{M}_1 \cdot (\vec{\omega}_{foot} - \vec{\omega}_{shank}) + \vec{F}_1 \cdot (\vec{\omega}_{shank} \times \vec{r}_{shank,2}) + \vec{F}_{shank,2} \cdot (\vec{\omega}_{shank} \times \vec{r}_{shank,2})$$



$$P_{joint,6DOF} = \overrightarrow{M_d} \cdot \overrightarrow{\omega_d} + \overrightarrow{M_p} \cdot \overrightarrow{\omega_p} + \overrightarrow{F_d} \cdot \overrightarrow{v_d} + \overrightarrow{F_p} \cdot \overrightarrow{v_p}$$
Rotational Power Translational Power

$$P_{joint,trans} = \vec{F}_1 \cdot \vec{v}_1 + \vec{F}_2 \cdot \vec{v}_2$$

$$\sum \vec{F} = m \cdot \vec{a}$$

$$\vec{F}_1 = -\vec{F}_2$$

$$P_{joint,trans} = \vec{F}_1 \cdot (\vec{v}_1 - \vec{v}_2)$$

#### **6 DOF Joint Power**

$$P_{joint,6DOF} = P_{joint,rot} + P_{joint,trans}$$

$$= \overrightarrow{M}_1 \cdot (\overrightarrow{\omega}_{foot} - \overrightarrow{\omega}_{shank}) + \overrightarrow{F}_1 \cdot (\overrightarrow{v}_1 - \overrightarrow{v}_2 + \overrightarrow{\omega}_{shank} \times \overrightarrow{r}_{shank,2} / foot,1})$$

#### **6 DOF Joint Power**

$$P_{joint,6DOF} = P_{joint,rot} + P_{joint,trans}$$

$$= \overrightarrow{M}_1 \cdot (\overrightarrow{\omega}_{foot} - \overrightarrow{\omega}_{shank}) + \overrightarrow{F}_1 \cdot (\overrightarrow{v}_1 - \overrightarrow{v}_2 + \overrightarrow{\omega}_{shank} \times \overrightarrow{r}_{shank,2} / foot,1})$$

Side Note 1:

Why moments and forces on the foot (distal body)?

These parameters are innately provided by V3D

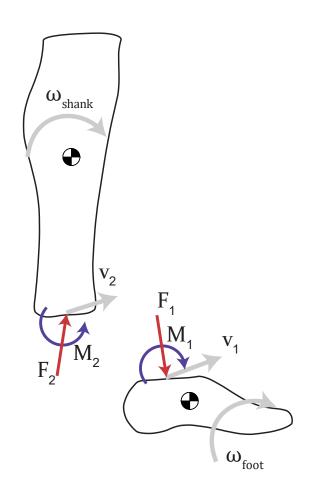
#### **6 DOF Joint Power**

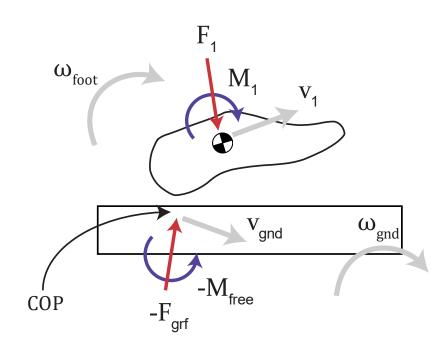
$$P_{joint,6DOF} = P_{joint,rot} + P_{joint,trans}$$

$$= \vec{M}_1 \cdot (\vec{\omega}_{foot} - \vec{\omega}_{shank}) + \vec{F}_1 \cdot (\vec{v}_1 - \vec{v}_2 + \vec{\omega}_{shank} \times \vec{r}_{shank,2})$$

Side Note 2: Is this a velocity term?

This looks like a rigid body velocity term... however, it is a consequence of rearranging our equations.

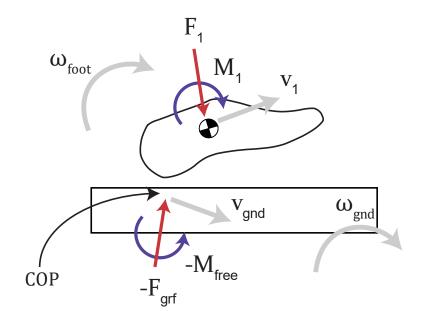




$$P_{joint,6DOF} = P_{joint,rot} + P_{joint,trans}$$

$$= \vec{M}_d \cdot (\vec{\omega}_d - \vec{\omega}_p) + \vec{F}_d \cdot (\vec{v}_d - \vec{v}_p + \vec{\omega}_p \times \vec{r}_{p/d})$$

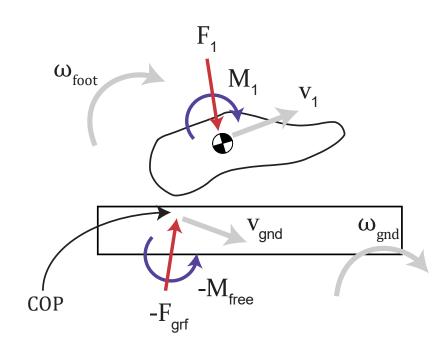
$$= -\vec{M}_{free} \cdot (\vec{\omega}_{gnd} - \vec{\omega}_{foot}) - \vec{F}_{grf} \cdot (\vec{v}_{gnd} - \vec{v}_{foot} + \vec{\omega}_{foot} \times \vec{r}_{foot})$$



$$P_{joint,6DOF} = P_{joint,rot} + P_{joint,trans}$$

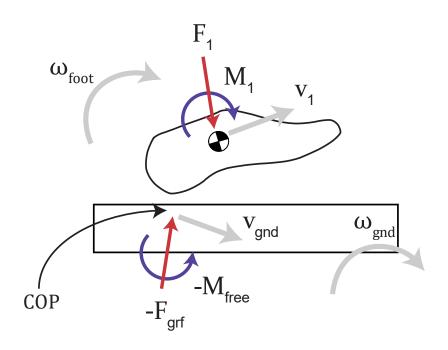
$$0$$

$$= -\vec{M}_{free} \cdot (\vec{\omega}_{gnd} - \vec{\omega}_{foot}) - \vec{F}_{grf} \cdot (\vec{v}_{gnd} - \vec{v}_{foot} + \vec{\omega}_{foot} \times \vec{r}_{foot}/_{COP})$$



$$P_{joint,6DOF} = P_{joint,rot} + P_{joint,trans}$$

$$P_{DistalFoot} = \vec{F}_{grf} \cdot (\vec{v}_{foot} + \vec{\omega}_{foot} \times \vec{r}_{COP}) + \vec{M}_{free} \cdot \vec{\omega}_{foot}$$



#### Hands-on Session

#### Hands-on Session

- Slack:
  - Channel: #tutorial-resources-files
  - Download & extract: DistalPower\_Workshop\_code\_files.zip
- Open "WorkshopCode\_fillin.m" in MATLAB

## Code: Computing Distal Segment Power

```
function Dist_Seg_Pow = DIST_SEG_POWER(Seg_COM_Vel,Seg_Ang_Vel,Seg_COM_Pos,CenterOfPressure,FreeMoment,GRF,treadmill yn,foot_vel)
  during gait.
  Parameters
  FreeMoment = Free moment on force platform in the lab coordinate system
  GRF = Ground Reaction Force in the lab coordinate system
  treadmill yn = 0 if overground, 1 if on the treadmill
  foot vel = velocity of the foot on the ground. It is NOT recommended to
   use the velocity readout from the treadmill while walking.
  Returns
 the treadmill belt
if treadmill yn == 1
    adj_Seg_COM_Vel = Seg_COM_Vel-ones(length(Seg_COM_Vel),1)*foot_vel;
end
Vel_COP_COM = adj_Seg_COM_Vel+cross(Seg_Ang_Vel,(CenterOfPressure-Seg_COM_Pps),2);
Dist Seg Pow = dot(GRF, Vel COP COM, 2) + dot(FreeMoment, Seg Ang Vel, 2);
end
```

## Code: Computing Distal Segment Power

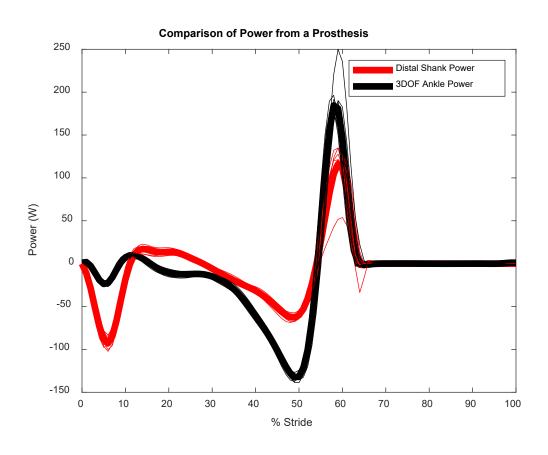
```
function Dist_Seg_Pow = DIST_SEG_POWER(Seg_COM_Vel,Seg_Ang_Vel,Seg_COM_Pos,CenterOfPressure,FreeMoment,GRF,treadmill_yn,foot_vel
  during gait.
  Parameters
  FreeMoment = Free moment on force platform in the lab coordinate system
  GRF = Ground Reaction Force in the lab coordinate system
  treadmill yn = 0 if overground, 1 if on the treadmill
   use the velocity readout from the treadmill while walking.
  Returns
 the treadmill belt
if treadmill yn == 1
    adj_Seg_COM_Vel = Seg_COM_Vel-ones(length(Seg_COM_Vel),1)*foot_vel;
end
Vel_COP_COM = adj_Seg_COM_Vel+cross(Seg_Ang_Vel,(CenterOfPressure-Seg_COM_Pps),2);
Dist Seg Pow = dot(GRF, Vel COP COM, 2) + dot(FreeMoment, Seg Ang Vel, 2);
end
```

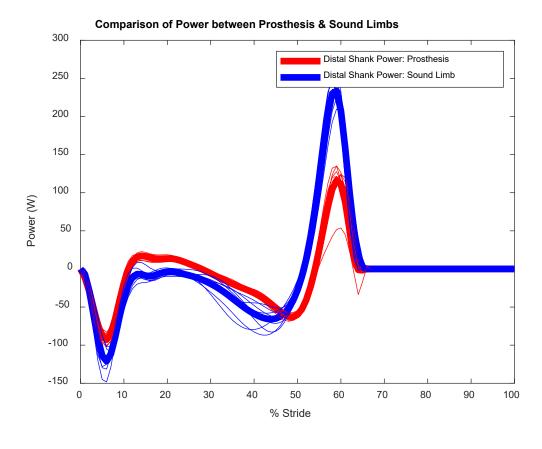
```
function foot vel = foot vel treadmill(HS,Speed,Foot Vel)
 This function is used to compute the velocity of the foot on the ground.
 When computing distal "segement" power during walking, it is encouraged
 to compute the treadmill velocity based on foot segment kinematics (or
  foot markers). The treadmill velocity is computed from "foot flat" which
 Parameters
   Array of heel strikes indicies can be either left or right
    (This variable is for debugging purposes)
debug = 0; % 1 to compare treadmill velocity and foot velocity
 When using a treadmill when computing distal segment power it is
 be an artificial power term within the computation. In order to do this,
 it is approximated by the foot flat variable when the foot is on the
 treadmill and moving at the pace of the treadmill backwards.
foot_flat = [.2,.4];
for ii = 1:(length(HS)-1)
    strideframe = HS(ii+1)-HS(ii);
   vel_foot_flat = (HS(ii)+round(foot_flat(1)*strideframe)):(HS(ii)+round(foot_flat(2)*strideframe));
    stride foot velocity(ii,:) = mean(Foot Vel(vel foot flat,:));
 Debug mode: Show estimated velocity vs. treadmill velocity
if debug == 1
    figure(1010)
end
foot vel = mean(stride foot velocity,1);
end
```

## Treadmill speed?

```
plot(1:length(stride_foot_velocity(:,1)),Speed*ones(1,length(stride_foot_velocity(:,1))),1:length(stride_foot_velocity(:,1)),rssq(stride_foot_velocity,2),'r')
```

## Evaluating prosthesis energy storage & return



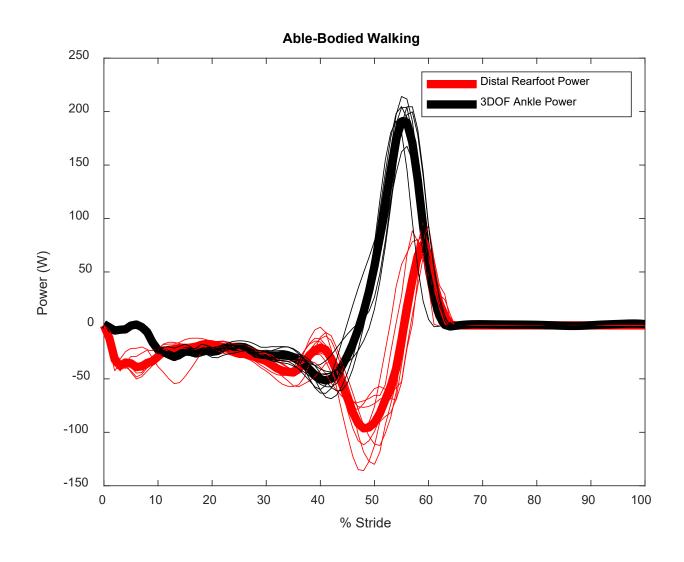


## Your turn! Able-Bodied Data or your Data

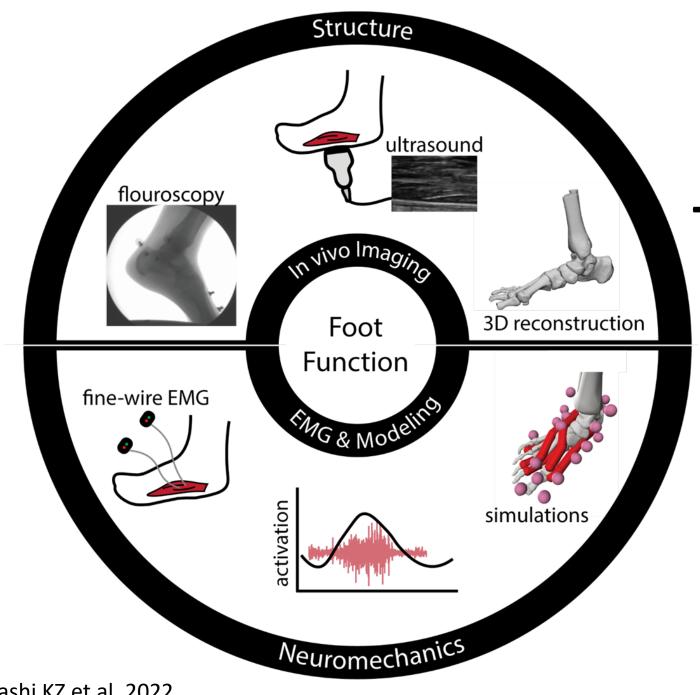
#### Goal:

- Create a comparison plot between distal rearfoot (hindfoot) and 3DOF ankle power
- Submit a screenshot of your plots to slack under #participant-uploads

## Able-Bodied Walking: Distal Rearfoot Power

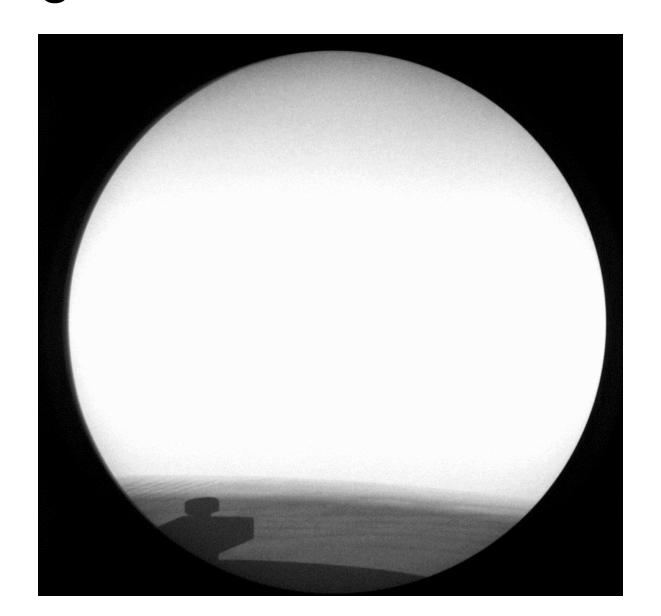


## **Future Directions**



## **Towards tissue-level** understanding

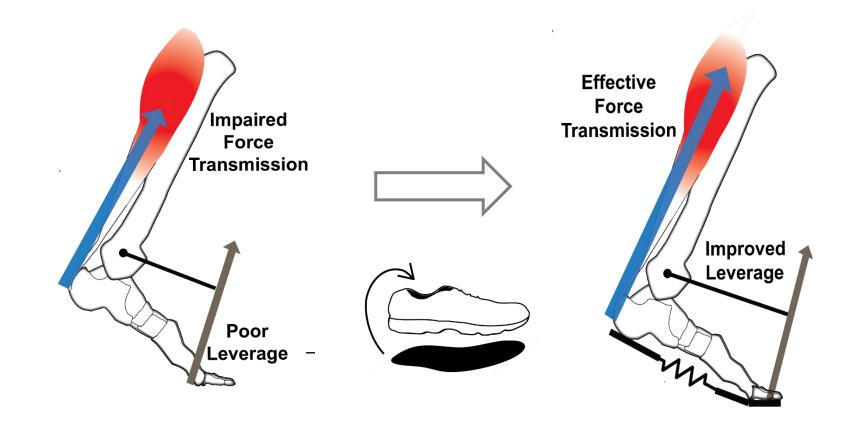
## Imaging feet inside shoes and insoles



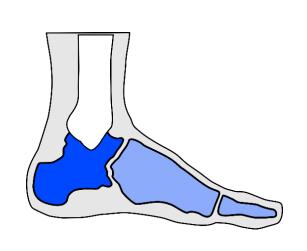
Biplane fluoroscopy from Dr. Amy Lenz lab (University of Utah)

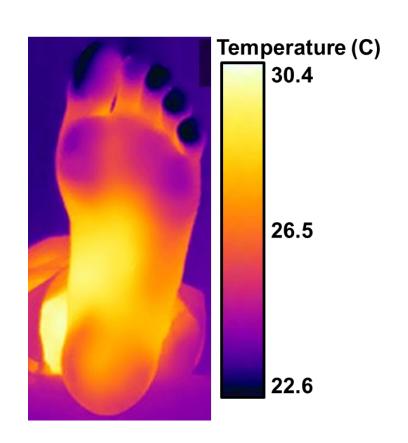
## **Enhancing Foot Function and Mobility**

Shoes + Insoles to reduce foot energy loss in older adults



# Foot energy loss -> heat dissipation?





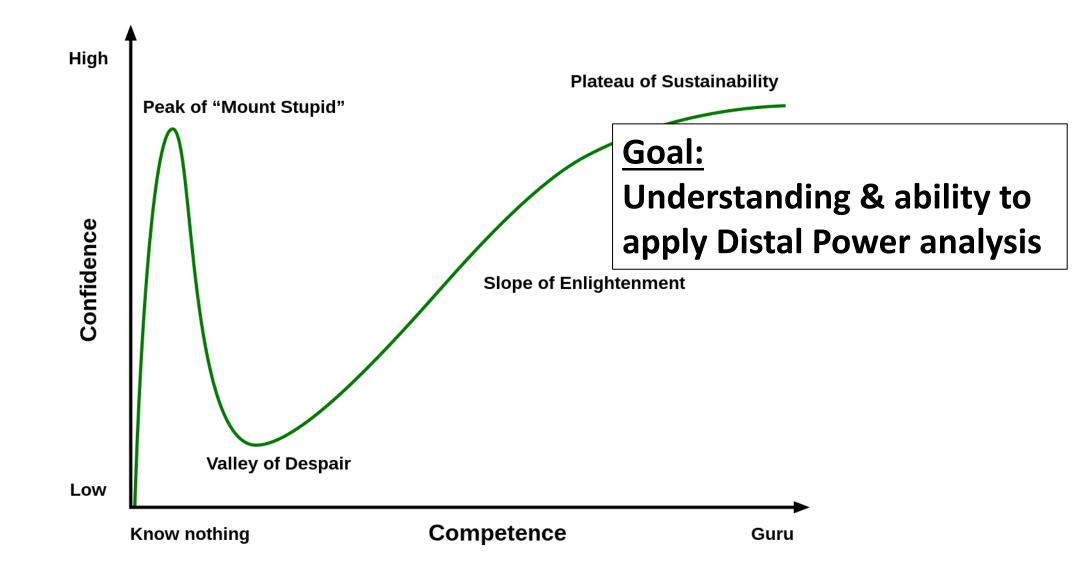


**Diabetic Ulcers** 

# Comparing structures across species and artificial limbs



## Workshop Goal: Slope of Enlightenment



#### Acknowledgements







#### **Collaborators**:

Tom Kepple (C-Motion Inc.) Steven Stanhope (University of Delaware) Karl Zelik (Vanderbilt University)